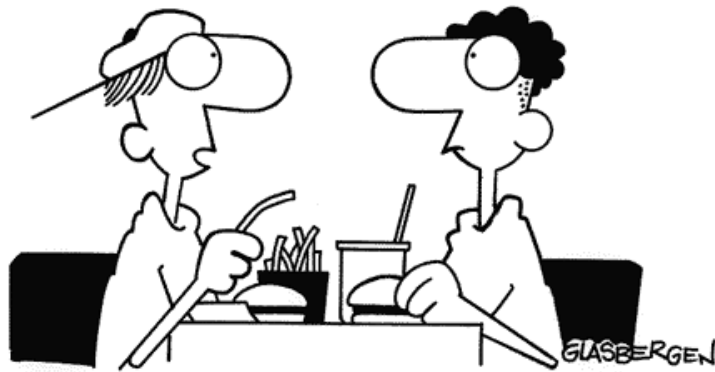


# 3-3

## Proving Lines Parallel

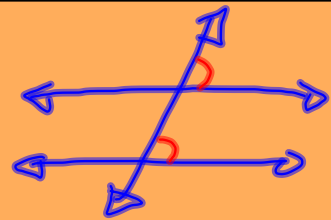
©1997 by Randy Glasbergen. E-mail: [randyg@norwich.net](mailto:randyg@norwich.net)  
<http://www.norwich.net/~randyg/toon.html>



**"I forgot to make a back-up copy of my brain,  
so everything I learned last semester was lost."**

Postulate 15 and Thm 3.1 - 3.3 are used when given  $\parallel$  lines to prove  $\sphericalangle$ 's or supplementary.

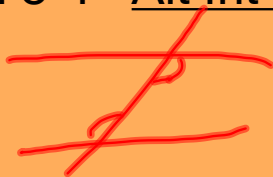
Use the following to prove lines  $\parallel$ :



Post 16 Corr  $\sphericalangle$ 's Converse

Corr.  $\sphericalangle$ 's  $\parallel$  lines

Thm 3-4 Alt Int  $\sphericalangle$  Converse



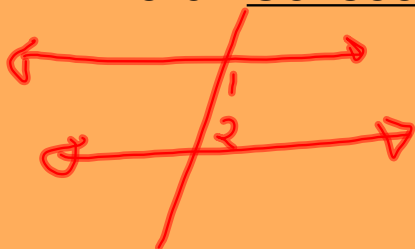
alt int  $\sphericalangle$ 's  $\parallel$  lines

Thm 3-5 Alt Ext  $\sphericalangle$  Converse



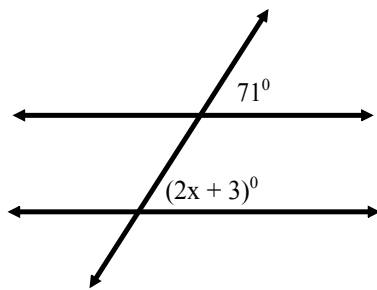
alt ext  $\sphericalangle$ 's  $\parallel$  lines

Thm 3-6 Consecutive Int  $\sphericalangle$  Converse



cons int  $\sphericalangle$ 's Supp  $\parallel$  lines

Find the value of  $x$  that makes  $m \parallel n$ .

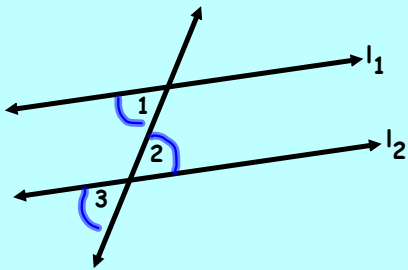


$$\begin{aligned} 2x + 3 &= 71 \\ -3 \quad -3 & \\ \hline 2x &= 68 \\ \frac{2x}{2} &= \frac{68}{2} \\ x &= 34 \end{aligned}$$

**Proof of Alt Int  $\angle$ 's Converse**

**Given:**  $\angle 1 \cong \angle 2$

**Prove:**  $l_1 \parallel l_2$



1.  $\angle 1 \cong \angle 2$
2.  $\angle 2 \cong \angle 3$
3.  $\angle 1 \cong \angle 3$
4.  $l_1 \parallel l_2$

1. Given
2. Vertical Angle Theorem
3. Transitive Property
4. Corresponding  $\angle$ 's Converse

**Given**

Ruler Postulate

Segment Addition Postulate

Protractor Postulate

Angle Addition Postulate

Reflexive Property

Symmetric Property

Transitive Property

Substitution Property

Vertical Angle Theorem

Linear Pair Postulate

Supplementary Angles

Complementary Angles

Congruent Supplement Theorem

Congruent Complements Theorem

If 2 lines  $\perp$  4 rt.  $\angle$ 's

All right  $\angle$ 's are

2 lines intersect to form a pair of adjacent  $\angle$ 's, the lines are .

Corresponding  $\angle$ 's Post.

Alternate Interior  $\angle$ 's Thm.

Consecutive Interior Angles Thm.

Alternate Exterior Angles Thm.

Perpendicular Transversal Thm.

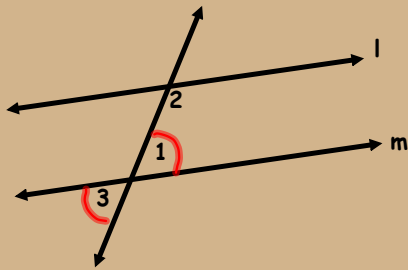
Corresponding  $\angle$ 's Converse

Alt Int  $\angle$ 's Converse

Consecutive Interior  $\angle$ 's Converse

Alternate Exterior  $\angle$ 's Converse

Given:  $\angle 3$  is supp to  $\angle 2$   
 Prove:  $l \parallel m$



1.  $\angle 3$  is supp to  $\angle 2$
2.  $\angle 3 \cong \angle 1$
3.  $\angle 1$  is supp to  $\angle 2$
4.  $l \parallel m$

1. Given
2. Vertical Angle Theorem
3. Substitution Property
4. Consecutive Interior  $\angle$ 's Converse

- Given
- Ruler Postulate
- Segment Addition Postulate
- Protractor Postulate
- Angle Addition Postulate
- Reflexive Property
- Symmetric Property
- Transitive Property
- Substitution Property
- Vertical Angle Theorem
- Linear Pair Postulate
- Supplementary Angles
- Complementary Angles
- Congruent Supplement Theorem
- Congruent Complements Theorem

If 2 lines  $\perp$  4 rt.  $\angle$ 's

All right  $\angle$ 's are

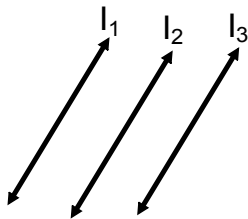
2 lines intersect to form a pair of adjacent  $\angle$ 's, the lines are .

- Corresponding  $\angle$ 's Post.
- Alternate Interior  $\angle$ 's Thm.
- Consecutive Interior Angles Thm.
- Alternate Exterior Angles Thm.
- Perpendicular Transversal Thm.

- Corresponding  $\angle$ 's Converse
- Alt Int  $\angle$ 's Converse
- Consecutive Interior  $\angle$ 's Converse
- Alternate Exterior  $\angle$ 's Converse

### Thm 3-1 Transitivity or Parallel Lines

If 2 lines are parallel to the same line, then they are parallel to each other.



$$l_1 \parallel l_2 \parallel l_3$$

Homework:

p. 165-169/1, 3-8, 10-15, 19-21

